

American University of Beirut

Department of Civil and Environmental Engineering

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NAME: Mr. Solution _____

ID: CIVE210 Exam I _____

CIVE 210 Statics	Exam I 1 1/2 Hour Exam	Sat Apr 4, 09 Closed Books	1/1
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Problem #1: (50%)

The crane ABC consists of 3 rigid, weightless and straight bars AB, BC and AC. The crane is lifting a mass M with a weightless cable connected to C. A spring having $K = 30\text{Kg/cm}$ tie point B back to a rigid support at point D.

Assume:

- 1- Bar AC and AB make angles 30° and 60° respectively with the horizontal
- 2- BD is perpendicular to AB
- 3- Hinge support at A
- 4- Length AB = 2m, BC = 4m
- 5- Drawing is not to scale.

Answer the following:

- a- Draw the Free Body Diagram and indicate clearly all necessary information (10%)

- b- Determine the tension force in spring DB in terms of M (15%)

$$\sum M@A = 0 \rightarrow T_s * AB = M * AC * \cos(30) \rightarrow T_s = 1.5 * M$$

- c- Assuming the tension force capacity in the cable holding M at C is 10Kg and the tension force capacity of the spring BD is 12Kg, determine the maximum mass M that can be carried (10%)

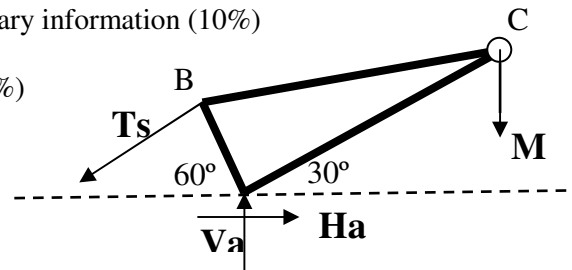
$$M = T_{\text{cable}} = 10\text{Kg} \rightarrow T_s = 15\text{Kg} > 12\text{Kg capacity} \rightarrow T_s = 12\text{Kg} \ \& \ M = 8\text{Kg}$$

- d- In part C, determine the corresponding spring force and corresponding deformation. Indicate magnitudes, tension or compression, shortening or elongation (5%)

$$T_s = 12\text{Kg (Tension)} \rightarrow \Delta = 12/30 = 0.4\text{cm (Elongation)}$$

- e- In part C, determine the corresponding reactions at A. Indicate magnitudes and directions. (15%)

$$\sum F_x = 0 \rightarrow H_a = T_s * \cos(30) = 10.4\text{Kg} \rightarrow H_a, \sum F_y = 0 \rightarrow V_a = T_s * \sin(30) + 8 = 14\text{Kg} \uparrow = V_a$$



Problem #2: (50%)

The rigid, weightless and straight bar ABC is roller supported at A and B over a circular path of radius $R = 24\text{m}$ and subjected to a pair of forces P and F. P is acting at a point G located in the middle of segment AB oriented perpendicular to AB, F is acting at tip C oriented at an angle α to the direction of bar ABC as shown.

Assume:

- 1- The magnitude of $P = 60\text{N}$
- 2- Frictionless and dimensionless roller supports A and B
- 3- Length AB = 12m, BC = 6m
- 4- Drawing is not to scale.

Answer the following:

- a- Draw the Free Body Diagram and indicate clearly all necessary information (10%)

$$OP = \sqrt{24^2 - 6^2} = 23.24, \text{ angle } OAP = \cos^{-1}(6/24) = 75.52^\circ$$

- b- Determine the minimum force F required for equilibrium and the corresponding angle α and reactions at A and B. Indicate magnitudes and directions (25%)

$$N_a, N_b \text{ and } P \text{ passes through center of circle. } \sum M@O = 0 \rightarrow F * dF = 0 \rightarrow \text{Minimum } F = 0, \alpha = \text{any}$$

$$N_a = N_b = 60 / (2 * \sin 75.52) = 30.98 = N_a = N_b$$

- c- Determine the minimum force F required to cause roller at B to barely touch the ground (reaction at B = 0) and the corresponding reaction at A. Indicate magnitudes and directions (15%)

$$\sum M@O = 0 \rightarrow F \text{ passes thru } O \rightarrow \alpha = \tan^{-1}(OP/PC) = \tan^{-1}(23.24/12) = 62.69^\circ = \alpha$$

$$\sum F_x = 0 \rightarrow F * \cos \alpha = N_a * \cos 75.52 \rightarrow N_a = 1.84 * F$$

$$\sum F_y = 0 \rightarrow F * \sin \alpha + N_a * \sin 75.52 = 60 \rightarrow F = 22.5\text{N}, N_a = 41.4\text{N}$$

